

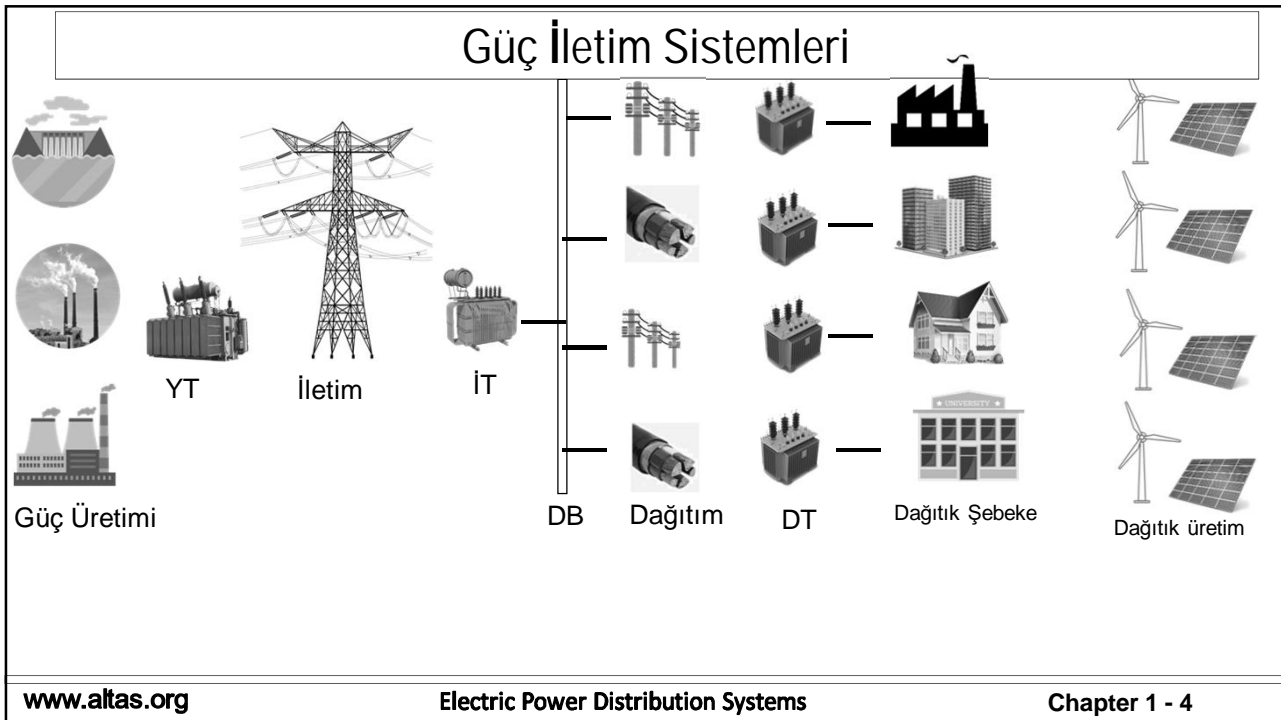
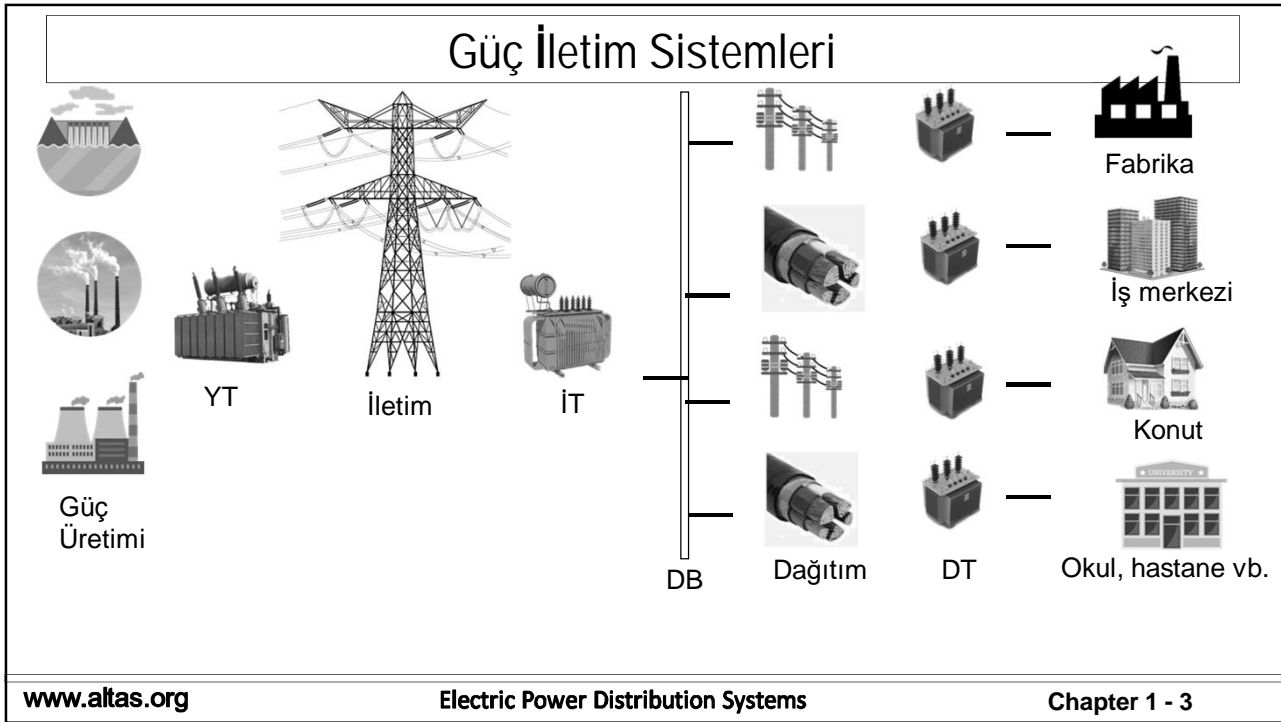
Electric Power Distribution Systems

Chapter 1 – Introduction

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Fundamentals of Power Systems

PROBLEMS

QUESTION

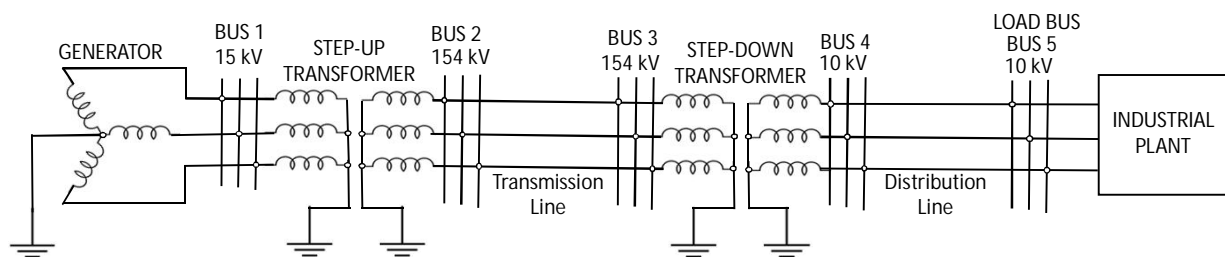
A power transmission system consists of a three-phase 15 kV generator, a step-up transformer, a 154 kV transmission line, a step-down transformer, a 10 kV distribution line, a load bus and an industrial plant. Three-phase stator windings of the generator are connected in wye. Step-up and step-down transformers are also both connected in wye-wye. The neutral points of all wye connections are solidly grounded.

- Draw a three-phase open circuit connection diagram of the system described above
- Draw a single line diagram of this system.

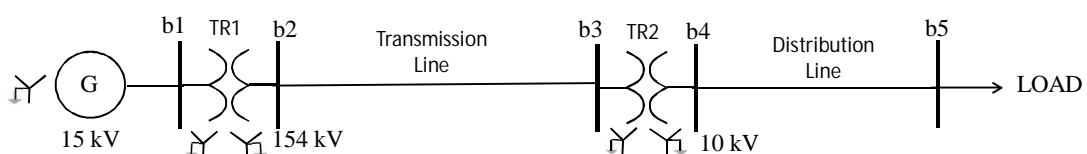
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PROBLEMS

Three-phase open circuit diagram



Single-line diagram



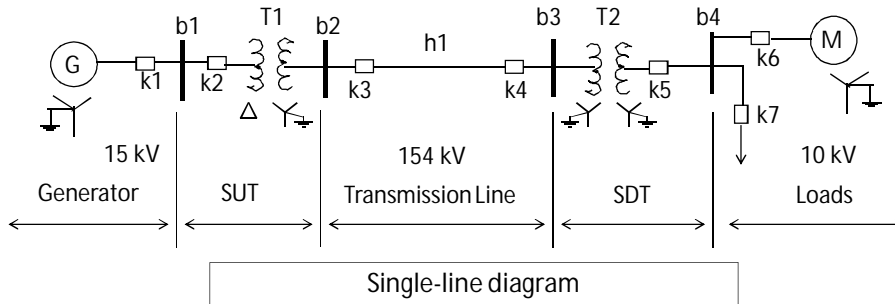
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PROBLEMS

QUESTION

A single line power system shown in Figure consists of main components from generation to dissipation.

Draw an impedance diagram of this system.

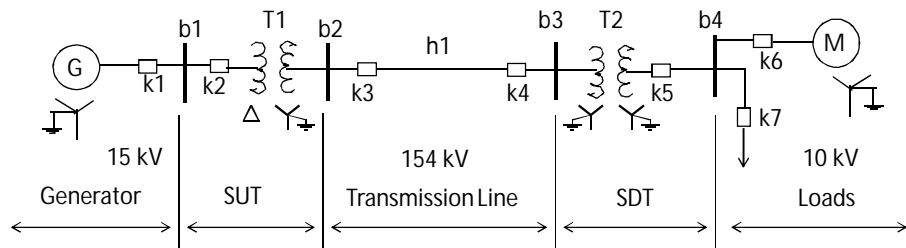


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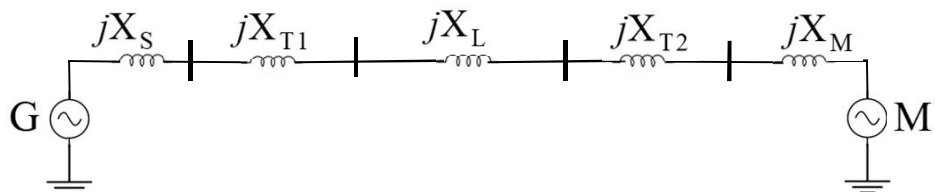
PROBLEMS

ANSWER

Single-line diagram

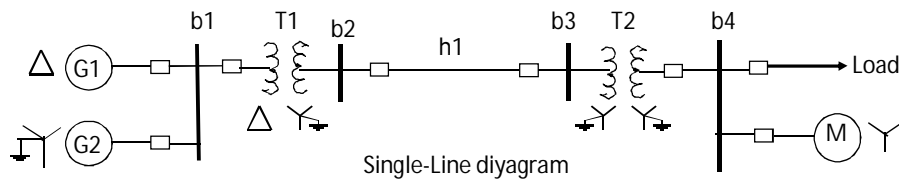


Impedance diagram



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PROBLEMS



DATA USED IN SINGLE-LINE DIAGRAMS

Generator G1

30 MVA
13,8 kV
X=%8

Generator G2

20 MVA
13,8 kV
X=%10

Transmission Line h1

$Z_h = 2 + j3 \Omega/\text{km}$
l = ... km

Motor M

10 MVA
6,6 kV
X=%12

Senkron (dinamik)
Kondansatör

Transformer T1

50 MVA
13,8 kV Δ / λ 138 kV
X=%5

Transformer T2

20 MVA
79,7 kV λ / λ 3,81 kV
X=%6

Load

40 MW
6,6 kV
0,80 geri

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PROBLEMS

DATA USED IN SINGLE-LINE DIAGRAMS

Generator Data

S_N : Nominal power
 U_N : Nominal line voltage
%X : Reactance and resistance of the windings in percentages.
Connection type of the windings

Transmission Lines

Line impedance or total impedance per km.

Load

P_N active power
 U_N nominal line-to-line voltage
Power factor

Transformers

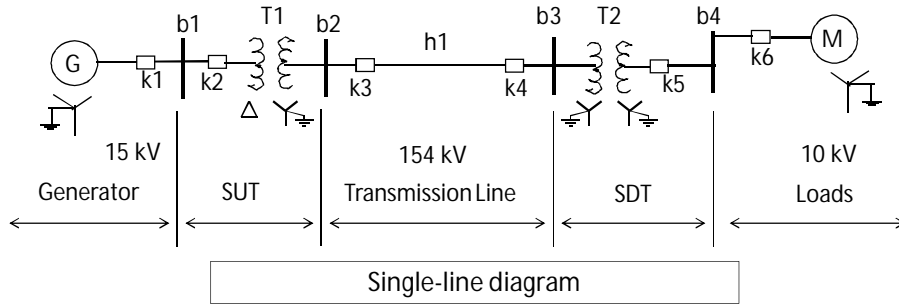
S_N : Nominal 3-phase power
 U_{N1} ve U_{N2} : Nominal input/output voltages
%X : Reactance and resistance of the windings in percentages.
Connection type of the windings

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PROBLEMS

QUESTION

Obtain the impedance diagram of the power system represented by following single-line diagram. Show each step.

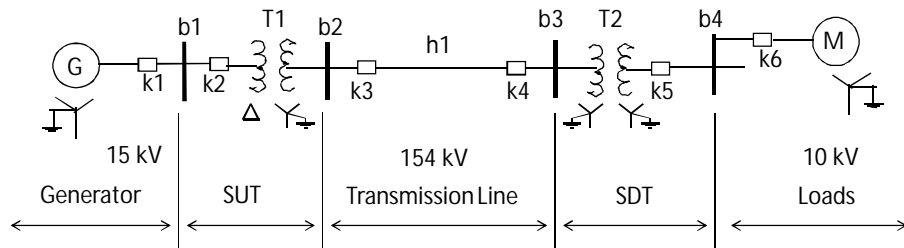


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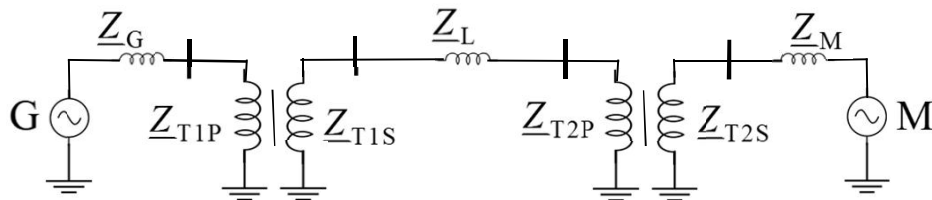
PROBLEMS

ANSWER

Single-line diagram



Impedance diagram

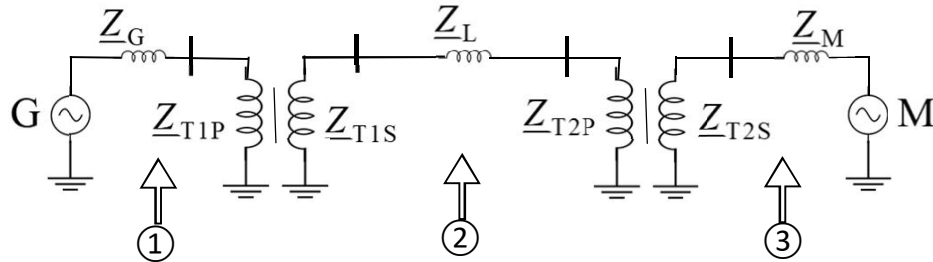


Very complicated?

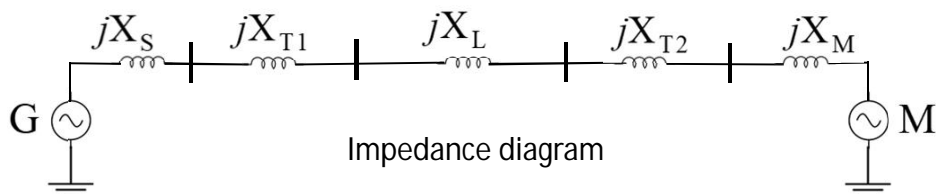
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PROBLEMS

ANSWER



There are three voltage circuits. These different voltage levels must be considered when constructing the impedance diagram given below. This issue will be discussed in next examples.



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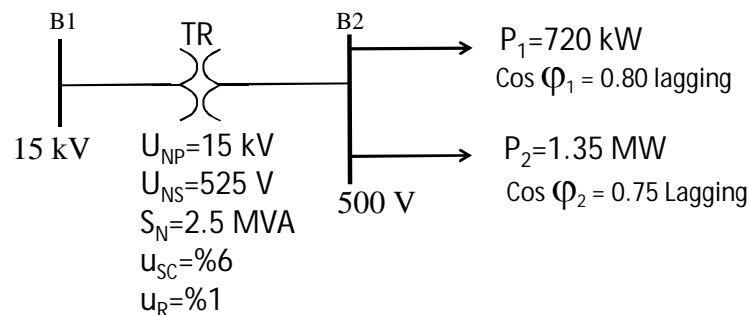
Chapter 1 - 13

Fundamentals of Power Systems

PROBLEMS

QUESTION

Two separate loads with $P_1=720$ kW power and 0.75 lagging power factor and $P_2=1.35$ MW power with 0.80 lagging power factor are fed over a 15/0.525 kV, 2.5 MVA transformer as shown in the figure. The voltage of the busbar B_1 is kept constant at $U_{B1}=15$ kV. Create the impedance diagram for this system.



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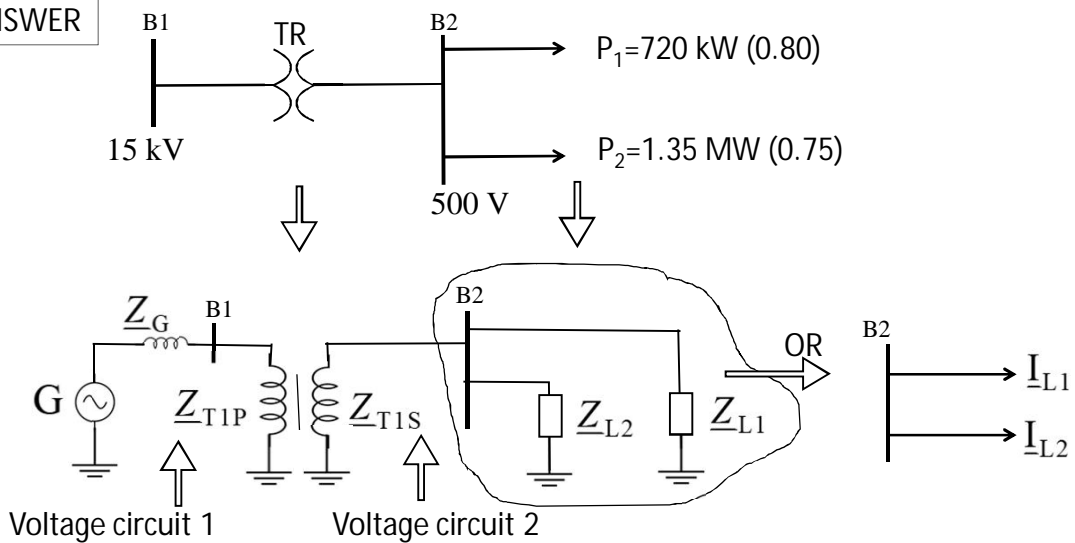
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Chapter 1 - 14

Fundamentals of Power Systems

PROBLEMS

ANSWER



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Chapter 1 - 15

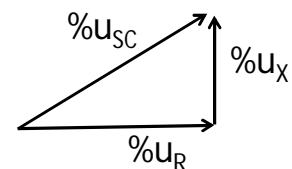
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PROBLEMS

ANSWER

- There are two different voltage circuits in this system.
- One of these voltage circuits should be selected as the operating circuit and the values in the other circuit should be transferred to this operating circuit.
- $\%u_{SC}$ and $\%u_R$ values are given in the figure as transformer data.

ASIDE

What are $\%u_{SC}$ and $\%u_R$ $\%u_{SC}$: Short circuit voltage. $\%u_R$: The voltage that causes Cooper losses under full load. $\%u_X$: The voltage that causes magnetizing losses under full load.

$$\%u_X = \sqrt{(\%u_{SC})^2 - (\%u_R)^2}$$

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Chapter 1 - 16

Fundamentals of Power Systems

PROBLEMS

ANSWER The impedance values of the transformer on LV side:

$$R_{TLV} = \%u_R \frac{U_{NLV}^2}{100S_N} = (1) \frac{0.525^2}{100 \times 2.5} = 0.0011 \Omega$$

$$\%u_X = \sqrt{(\%u_{SC})^2 - (\%u_R)^2} = \sqrt{6^2 - 1^2} = 5.916$$

$$X_{TLV} = \%u_X \frac{U_{NLV}^2}{100S_N} = 5.916 \frac{0.525^2}{100 \times 2.5} = 0.0065 \Omega$$

Z @ LV

$$\underline{Z}_{TLV} = R_{TLV} + jX_{TLV} = 0.0011 + j0.0065 \Omega$$

Transformer impedance on
525 V LV side:

$$\underline{Z}_{TLV} = Z_{TLV} \angle \theta = 0.006592 \angle 80.39^\circ \Omega$$

Fundamentals of Power Systems

PROBLEMS

ANSWER The impedance values of the transformer on HV side:

$$R_{THV} = \%u_R \frac{U_{NHV}^2}{100S_N} = (1) \frac{15^2}{100 \times 2.5} = 0.9 \Omega$$

$$\%u_X = \sqrt{(\%u_{SC})^2 - (\%u_R)^2} = \sqrt{6^2 - 1^2} = 5.916$$

$$X_{THV} = \%u_X \frac{U_{NHV}^2}{100S_N} = 5.916 \frac{15^2}{100 \times 2.5} = 5.3244 \Omega$$

Z @ HV

$$\underline{Z}_{THV} = R_{THV} + jX_{THV} = 0.9 + j5.3244 \Omega$$

Transformer impedance on
15 kV HV side:

$$\underline{Z}_{THV} = Z_{THV} \angle \theta = 5.3999 \angle 80.39^\circ \Omega$$

Fundamentals of Power Systems

PROBLEMS

ANSWER The impedance values of the loads on LV side:

The loads P1 and P2 given in this problem are shown with their impedance equivalents. These loads could also be represented as load currents. Because these loads will draw constant current with their constant impedance at constant active power and power coefficient.

Power values per phase:

$$P_{1\phi} = \frac{P_{3\phi}}{3} \text{ kW/faz}$$

$$P_1 = \frac{720}{3} = 240 \text{ kW/faz}$$

$$P_2 = \frac{1.35}{3} = 0.45 \text{ MW/faz}$$

If the L-L voltage of the busbar B₂ is kept constant at 500 V, the phase-neutral voltage is then:

$$V_{LN} = \frac{U}{\sqrt{3}} = \frac{500}{\sqrt{3}} = 288.675 \text{ V}$$

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Chapter 1 - 19

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PROBLEMS

ANSWER The impedance values of the loads on LV side:

LOAD IMPEDANCES

$$Z_{L1LV} = \frac{V_{LN}}{I_{Ph}} = \frac{V_{LN}}{\frac{P_{1\phi}}{V_{LN} \cos \varphi_1}} = \frac{V_{LN}^2 \cos \varphi_1}{P_{1\phi}} = \frac{V_{LN}^2}{S_{1\phi}}$$

Z @ LV

$$Z_{L1LV} = \frac{V_{LN}^2 \cos \varphi_1}{P_{1\phi}} = \frac{\left(\frac{500}{\sqrt{3}}\right)^2}{240 \times 10^3} \times 0.80 = 0.277 \Omega$$

$$Z_{L2LV} = \frac{V_{LN}^2 \cos \varphi_1}{P_{1\phi}} = \frac{\left(\frac{500}{\sqrt{3}}\right)^2}{0.40 \times 10^6} \times 0.75 = 0.1389 \Omega$$

Impedances can also be calculated directly from 3-phase power and phase-to-phase voltages.

$$S_{L13\phi} = \frac{P_{L13\phi}}{\cos \varphi_1} = \frac{720}{0.80} = 900 \text{ kVA}$$

$$S_{L23\phi} = \frac{P_{L23\phi}}{\cos \varphi_1} = \frac{1.35}{0.75} = 1.8 \text{ MVA}$$

Z @ LV

$$Z_{L1LV} = \frac{U_{LL}^2}{S_{L13\phi}} = \frac{500^2}{900 \times 10^3} = 0.277 \Omega$$

$$Z_{L2LV} = \frac{U_{LL}^2}{S_{L23\phi}} = \frac{500^2}{1.8 \times 10^6} = 0.1389 \Omega$$

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Chapter 1 - 20

Fundamentals of Power Systems

PROBLEMS

ANSWER

The current values of the loads on LV side:

I @ LV

Load currents can also be used to represent loads instead of load impedances. Phase currents can be calculated directly using L-N voltages and powers per phase, or using 3-phase circuit values.

CURRENT

Using per-phase values:
$$I_{L1} = \frac{P_{L1\phi}}{V_{LN} \cos \phi_1} = \frac{240 \times 10^3}{(288.675)(0.80)} = 1039.23 \text{ A}$$

$$I_{L2} = \frac{P_{L2\phi}}{V_{LN} \cos \phi_2} = \frac{0.45 \times 10^6}{(288.675)(0.75)} = 2078.46 \text{ A}$$

Using three-phase values:

$$I_{L1} = \frac{P_{L13\phi}}{\sqrt{3} V_{LL} \cos \phi_1} = \frac{720 \times 10^3}{\sqrt{3} \times 500 \times 0.80} = 1039.23 \text{ A}$$

$$I_{L2} = \frac{P_{L23\phi}}{\sqrt{3} V_{LL} \cos \phi_2} = \frac{1.35 \times 10^6}{\sqrt{3} \times 500 \times 0.75} = 2078.46 \text{ A}$$

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Electric Power Distribution Systems

Chapter 1 - 21

Fundamentals of Power Systems

PROBLEMS

ANSWER

The current values of the loads on LV side:

I @ LV

CURRENT

Angles related to power coefficients given for loads:

$$\phi_1 = \cos^{-1}(0.80) = 36.86^\circ$$

$$\phi_2 = \cos^{-1}(0.75) = 41.4^\circ$$

Thus, the load currents can be expressed as phasors.

$$\underline{I}_{L1LV} = 1039.23 \angle -36.86^\circ \text{ A}$$

I @ LV

$$\underline{I}_{L2LV} = 2078.42 \angle -41.4^\circ \text{ A}$$

These are the load currents at low voltage side of the transformer.

These current values calculated for the 500 V low voltage circuit must be transferred to 15 kV circuit so that they can be used together with the Z_{THV} in the 15 kV high voltage circuit. This transfer can be accomplished using the transformer's turn ratio.

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Chapter 1 - 22

Fundamentals of Power Systems

PROBLEMS

ANSWER

The current values of the loads on HV side:

I @ HV

$$\frac{N_1}{N_2} = \frac{U_{NHV}}{U_{NLV}} = \frac{15 \text{ kV}}{0.525 \text{ kV}} = \frac{I_{NLV}}{I_{NHV}} \Rightarrow I_{NHV} = I_{NLV} \frac{0.525 \text{ kV}}{15 \text{ kV}}$$

Ignoring the losses, we can assume that the power on both sides of the transformer would be equal.

$$U_{NHV} I_{NHV} = U_{NLV} I_{NLV}$$

$$I_{L1HV} = I_{L1LV} \frac{U_{NLV}}{U_{NHV}} = 1039.23 \angle -36.86^\circ \left(\frac{0.525}{15} \right) = 36.373 \angle -36.86^\circ \text{ A}$$

$$I_{L2HV} = I_{L2LV} \frac{U_{NLV}}{U_{NHV}} = 2078.42 \angle -41.4^\circ \left(\frac{0.525}{15} \right) = 72.7447 \angle -41.4^\circ \text{ A}$$

$$I_{L1HV} = 36.373 \angle -36.86^\circ \text{ A}$$

$$I_{L2HV} = 72.7447 \angle -41.4^\circ \text{ A}$$

I @ HV

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Chapter 1 - 23

Fundamentals of Power Systems

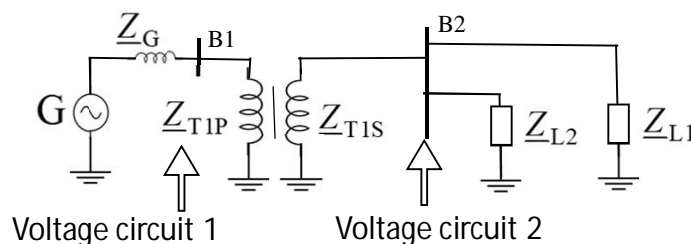
PROBLEMS

ANSWER

Configuring the impedance diagrams as separate circuits according to the voltage levels (lower and higher voltage sides) of the transformers makes the operations complicated and difficult. Therefore it is better to configure the impedance diagrams as a whole circuit instead of separating them into the lower and upper voltage circuits.

The impedance diagram can also be formed as a single circuit without using the per-unit values. However, in this case, all values in the circuit must be transferred to either the lower voltage circuit or the higher voltage circuit.

The next examples explain this issue.



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Chapter 1 - 24

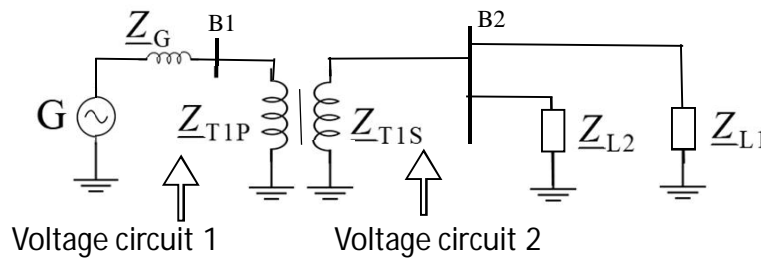
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PROBLEMS

QUESTION

Obtain and draw the Impedance diagram of the power system given in the previous example for the following voltage circuits.

- a. For low voltage circuit
- b. For the upper voltage circuit.

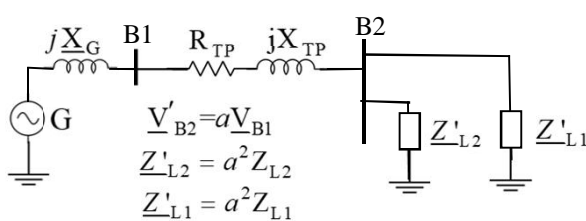
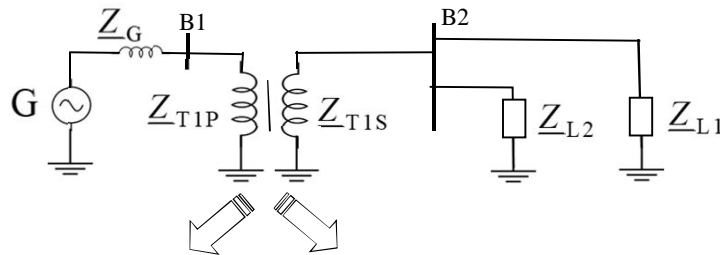


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PROBLEMS

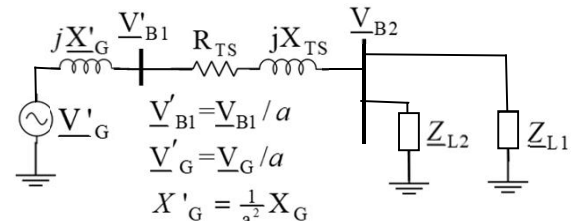
ANSWER

$$a = \frac{N_P}{N_S} = \frac{U_{NHV}}{U_{NLV}} = \frac{15}{0.525}$$



@ HV

Impedance diagram with all values at primary side (HV side for this example)



@ LV

Impedance diagram with all values at secondary side (LV side for this example)

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PROBLEMS

ANSWER

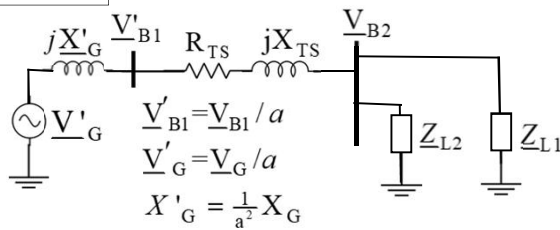
Obtain and write down all of the required circuit elements shown in the circuit @LV side.

From previous example:

$$Z_{TS} = Z_{TLV} = 0.0011 + j0.0065 \Omega$$

$$Z_{TS} = Z_{TLV} = 0.006592 \angle 80.39^\circ \Omega$$

@ LV



$$I_{L1} = 1039.23 \angle -36.86^\circ \text{ A}$$

$$I_{L2} = 2078.42 \angle -41.4^\circ \text{ A}$$

@ LV

Assume V_{B2} at reference

$$V_{B2} = \frac{500}{\sqrt{3}} \angle 0^\circ \text{ V}$$

@ LV

$$Z_{L1} = 0.277 \angle 36.86^\circ \Omega$$

$$Z_{L2} = 0.1389 \angle 41.4^\circ \Omega$$

@ LV

$$V'_{B1} = V_{B2} + (I_{L1} + I_{L2}) Z_{TS} \text{ Volt}$$

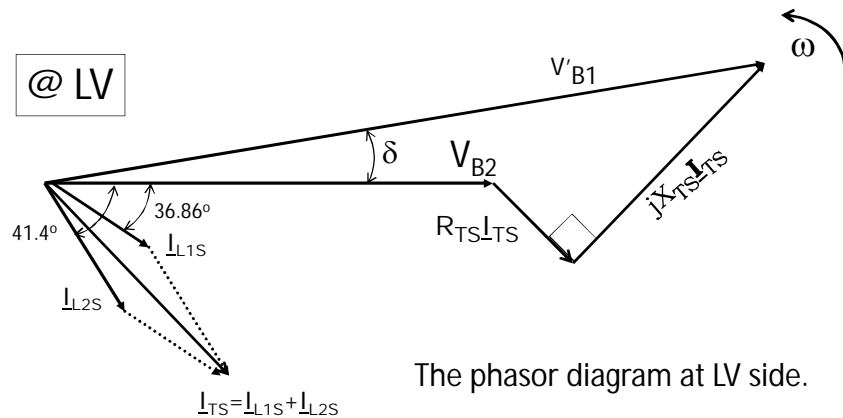
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PROBLEMS

ANSWER

Obtain and write down all of the required circuit elements shown in the circuit @LV side.

@ LV



Fundamentals of Power Systems

PROBLEMS

QUESTION

Obtain and write down all of the required circuit elements shown in the circuit @HV side. The PRIMARY.

@ HV

$$\underline{Z}_{\text{THV}} = R_{\text{THV}} + jX_{\text{THV}} = 0.9 + j5.3244 \Omega$$

$$a = \frac{15}{0.525}$$

$$\underline{Z}'_{\text{THV}} = \underline{Z}_{\text{THV}} \angle \theta = 5.3999 \angle 80.39^\circ \Omega$$

$$\underline{Z}'_{\text{TP}} = \underline{Z}_{\text{THV}} \angle \theta$$

$$\underline{I}_{\text{L1HV}} = 36.373 \angle -36.86^\circ \text{ A}$$

$$\underline{I}_{\text{L2HV}} = 72.7447 \angle -41.4^\circ \text{ A}$$

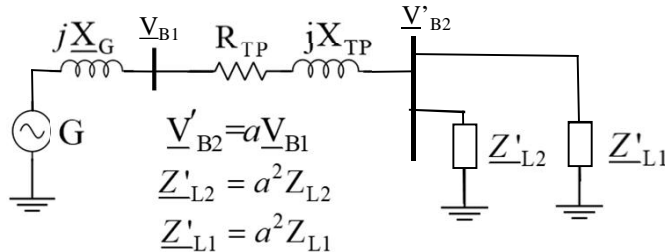
$$\underline{V}'_{\text{B2}} = \frac{500}{\sqrt{3}} \angle 0^\circ \text{ V reference}$$

$$\begin{aligned} \underline{Z}'_{\text{L1H}} &= a^2 0.277 \angle 36.86^\circ \Omega \\ &= 226.122 \angle 36.86^\circ \Omega \end{aligned}$$

$$\begin{aligned} \underline{Z}'_{\text{L2}} &= a^2 0.1389 \angle 41.4^\circ \Omega \\ &= 113.38 \angle 41.4^\circ \Omega \end{aligned}$$

@ HV

$$\underline{V}_{\text{B1}} = \underline{V}'_{\text{B2}} + (\underline{I}'_{\text{L1}} + \underline{I}'_{\text{L2}}) \underline{Z}'_{\text{TP}} \text{ Volt}$$



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Chapter 1 - 29

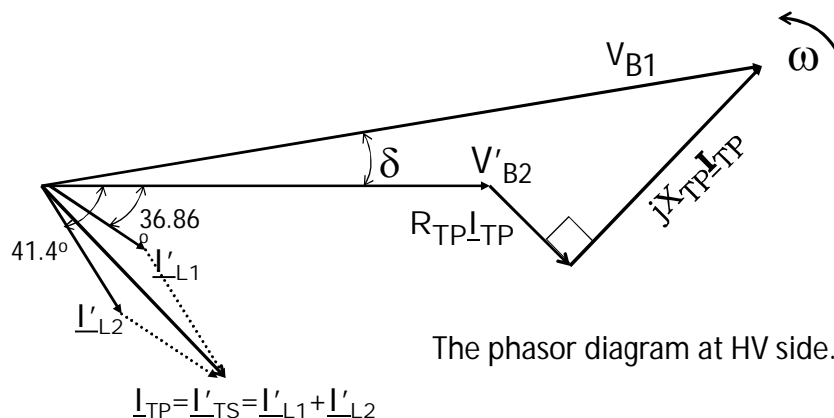
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PROBLEMS

ANSWER

Obtain and write down all of the required circuit elements shown in the circuit @HV side.

@ HV



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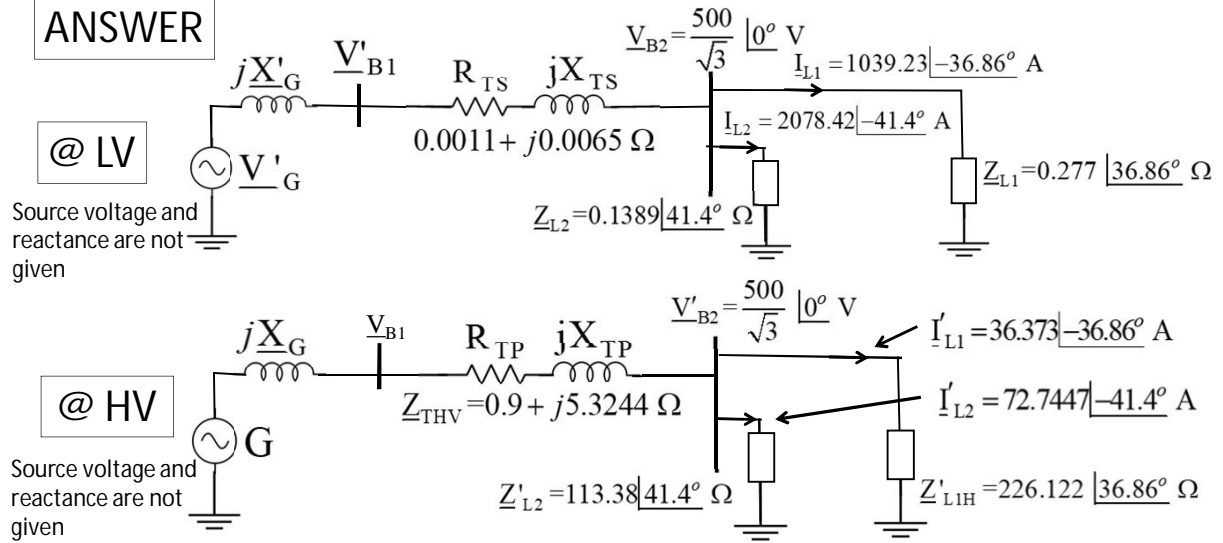
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Chapter 1 - 30

Fundamentals of Power Systems

PROBLEMS

ANSWER



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Chapter 1 - 31

Fundamentals of Power Systems

PROBLEMS

QUESTION

In the system whose impedance diagram is obtained in the previous example, if the voltage of the busbar B1 is kept constant at 15 kV, answer the following.

- What will be the voltage value of the B1 busbar?
- What is the power factor in the B1 and B2 busbars?

NOTE : Take the voltage of the B2 busbar as reference.

HINT: Since V_2 voltage is not known, I_1 and I_2 load currents can be written as dependent on V_2 voltage.

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Chapter 1 - 32

Fundamentals of Power Systems

PROBLEMS

ANSWER

$$I_{L1} = \frac{P_{L13\phi}}{\sqrt{3} V_{LLS} \cos \phi_1} = \frac{720 \times 10^3}{\sqrt{3} \times \sqrt{3} V_{LNS} \times 0.80} = \frac{300\,000}{V_{LNS}} \text{ A}$$

$$I_{L1} = \frac{300\,000}{V_{LNS}} \angle -36.87^\circ \text{ A} \quad @ \text{ LV}$$

$$I_{L2} = \frac{P_{L23\phi}}{\sqrt{3} V_{LLS} \cos \phi_2} = \frac{1.35 \times 10^6}{\sqrt{3} \times \sqrt{3} V_{LNS} \times 0.75} = \frac{600\,000}{V_{LNS}} \text{ A}$$

$$I_{L2} = \frac{600\,000}{V_{LNS}} \angle -41.4^\circ \text{ A} \quad @ \text{ LV}$$

$$\underline{Z}_{TS} = R_{TS} + jX_{TS} = 0.0011 + j0.0065 \Omega \quad @ \text{ LV}$$

$$\underline{I}_{TS} = \underline{I}_{L1} + \underline{I}_{L2} = \frac{300\,000}{V_{LNS}} \angle -36.87^\circ + \frac{600\,000}{V_{LNS}} \angle -41.4^\circ \text{ A.} \quad @ \text{ LV}$$

$$\underline{I}_{TS} = \underline{I}_{L1} + \underline{I}_{L2} = \frac{1}{V_{LNS}} (690\,000 - j576\,780) \text{ A.}$$

$$\underline{I}_{TS} = \frac{899\,319.2806}{V_{LNS}} \angle -39.89^\circ \text{ A.}$$

Fundamentals of Power Systems

PROBLEMS

ANSWER

Details

$$\underline{I}_{TS} = \underline{I}_{L1} + \underline{I}_{L2}$$

$$= \frac{300\,000}{V_2} (\cos 36.87^\circ - j \sin 36.87^\circ) + \frac{600\,000}{V_2} (\cos 41.4^\circ - j \sin 41.4^\circ)$$

$$= \frac{300\,000}{V_2} (0.80 - j0.60) + \frac{600\,000}{V_2} (0.75 - j0.6613)$$

$$= \frac{240\,000}{V_2} - j \frac{180\,000}{V_2} + \frac{450\,000}{V_2} - j \frac{396\,780}{V_2}$$

$$= \frac{690\,000}{V_2} - j \frac{576\,780}{V_2}$$

$$\underline{I}_{TS} = \frac{1}{V_{LNS}} (690\,000 - j576\,780) \text{ A.}$$

Fundamentals of Power Systems

PROBLEMS

ANSWER

@ LV

Voltage drop on transformer:

$$\underline{\Delta V}_{TS} = \underline{Z}_{TS} \underline{I}_{TS} = (0.00659 \angle 80.39^\circ) \left(\frac{899 \ 319.2806}{V_{LNS}} \angle -39.89^\circ \right)$$

$$\underline{\Delta V}_{TS} = \frac{5926.514}{V_{LNS}} \angle 40.5^\circ \quad @ \text{ LV}$$

The value of the busbar B1 voltage transferred to the low voltage circuit

$$\underline{\Delta V}'_{TP} = \underline{V}_{TS} + \underline{\Delta V}_{TS} \quad @ \text{ LV}$$

Since the B1 busbar voltage is constant at $U_1=15$ kV,

$$V_{TP} = \frac{15}{\sqrt{3}} = 8.66 \text{ kV} \quad @ \text{ HV}$$

This value will remain constant. Its transferred value to the low voltage circuit:

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Electric Power Distribution Systems

Chapter 1 - 35

Fundamentals of Power Systems

PROBLEMS

ANSWER

$$V'_{TP} = V_{TP} \left(\frac{U_{NS}}{U_{NP}} \right) = \frac{15}{\sqrt{3}} \left(\frac{0.525}{15} \right) = 0.3031 \text{ kV}$$

$$\underline{V}'_{TP} = 0.3031 \angle \delta \text{ kV}$$

$$\underline{V}'_{TP} = 303.1 \angle \delta \text{ V}$$

$$\underline{\Delta V}'_{TP} = \underline{V}_{TS} + \underline{\Delta V}_{TS}$$

$$303.1 \angle \delta = \underline{V}_{TS} + \frac{5956.514}{V_{TS}} \angle 40.5^\circ$$

$$303.1 \angle \delta = \underline{V}_{TS} + \frac{5956.514}{V_{TS}} (\cos 40.5^\circ + j \sin 40.5^\circ)$$

$$303.1 \angle \delta = \frac{V_{TS}^2 + 4504.15}{V_{TS}} + j \frac{3848.96}{V_{TS}}$$

@ LV

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Electric Power Distribution Systems

Chapter 1 - 36

Fundamentals of Power Systems

PROBLEMS

ANSWER

$$303.1 \angle \delta = \frac{V_{TS}^2 + 4504.15}{V_{TS}} + j \frac{3848.96}{V_{TS}}$$

$$303.1 = \sqrt{\left(\frac{V_{TS}^2 + 4504.15}{V_{TS}}\right)^2 + \left(\frac{3848.96}{V_{TS}}\right)^2}$$

$$(303.1)^2 = \left(\frac{V_{TS}^2 + 4504.15}{V_{TS}}\right)^2 + \left(\frac{3848.96}{V_{TS}}\right)^2$$

$$(303.1)^2 V_{TS} = (V_{TS}^2 + 4504.15)^2 + (3848.96)^2$$

$$(303.1)^2 V_{TS} = V_{TS}^4 + 2 \times 4504.15 V_{TS}^2 + (4504.15)^2 + (3848.96)^2$$

$$V_{TS}^4 + (2 \times 4504.15 - (303.1)^2) V_{TS}^2 + (4504.15)^2 + (3848.96)^2 = 0$$

$$V_{TS}^4 + (82861.31) V_{TS}^2 + 35101860.3 = 0$$

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Electric Power Distribution Systems

Chapter 1 - 37

Fundamentals of Power Systems

PROBLEMS

ANSWER

$$V_{TS}^4 + (82861.31) V_{TS}^2 + 35101860.3 = 0$$

$$\text{Let: } x = V_{TS}^2$$

$$x^2 + (82861.31)x + 35101860.3 = 0$$

$$x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{82861.31 \pm \sqrt{(82861.31)^2 - 4(1)(35101860.3)}}{2(1)}$$

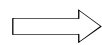
$$x_{1,2} = \frac{82861.31 \pm 82009.69}{2} \quad \Rightarrow \quad \begin{aligned} x_1 &= 82435.5 \\ x_2 &= 425.81 \end{aligned}$$

Since

$$x = V_{TS}^2$$

@ LV

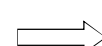
$$V_{TS1} = \sqrt{x_1}$$



$$V_{TS1} = 287.115 \text{ V}$$

SUITABLE

$$V_{TS2} = \sqrt{x_2}$$



$$V_{TS2} = 20.635 \text{ V}$$

NOT SUITABLE

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Electric Power Distribution Systems

Chapter 1 - 38

Fundamentals of Power Systems

PROBLEMS

ANSWER

Since $\underline{V}_{TS} = 287.115 \angle 0^\circ \text{ V}$

$$303.1 \angle \delta = \frac{(287.115)^2 + 4504.15}{287.115} + j \frac{3848.96}{287.115}$$

$$\left. \begin{aligned} 303.1 \angle \delta &= 302.8 + j13.4 \\ 303.1 \angle \delta &= 303.1 \angle 2.5^\circ \end{aligned} \right\} \delta = 2.5^\circ$$

Thus, if the busbar B1 voltage is kept constant at 15 kV, the relevant busbar voltages according to the lower voltage circuit are obtained as follows.

@ LV

$$\underline{V}'_{TP} = 303.1 \angle 2.5^\circ \text{ V.}$$

The power factor at busbar B1

$$\cos \phi_{B1} = \cos(39.89 + 2.5) = 0.738$$

$$\underline{V}_{TS} = 287.115 \angle 0^\circ \text{ V.}$$

The power factor at busbar B2

$$\cos \phi_{B2} = \cos(39.89) = 0.767$$

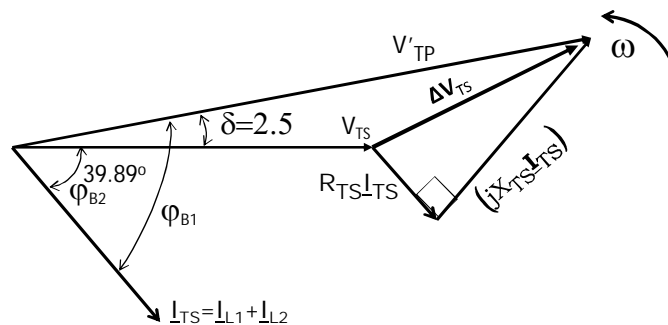
$$\underline{I}_{TS} = 3132.26 \angle -39.89^\circ \text{ A.}$$

Fundamentals of Power Systems

PROBLEMS

ANSWER

Fasor diagram @ LV



Fundamentals of Power Systems

PROBLEMS

QUESTION

The sub-transient synchronous reactance of a generator with a nominal value of 18 kV, 500 MVA is given as $X''=0.25$ pu. If the operations will be carried out at 20 kV, 100 MVA base values, what will be the pu value of the X'' reactance at this new base?

ANSWER

First find actual value in Ohm

$$X''_{\Omega} = X''_{pu} Z_{B1} \Rightarrow X''_{\Omega} = 0.25 \left(\frac{18^2}{500} \right)$$

Calculate new pu value with the new base $Z_{B2} = \frac{20^2}{100}$

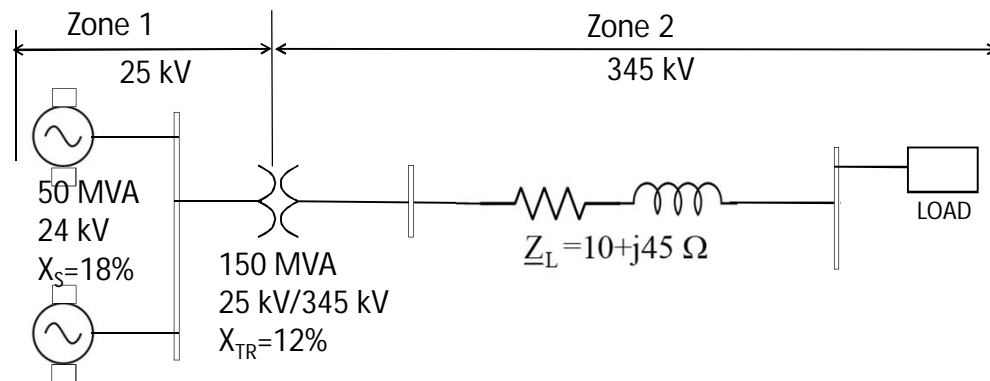
$$X''_{pu} = \frac{X''_{\Omega}}{Z_{B2}} = \frac{0.25 \left(\frac{18^2}{500} \right)}{\frac{20^2}{100}} = 0.25 \left(\frac{18^2}{500} \right) \times \frac{100}{20^2} = 0.0405$$

Fundamentals of Power Systems

PROBLEMS

QUESTION

A power system section with two voltage zones is given in the figure. The base values to be studied can be chosen randomly. However, choosing one of the nominal label values or values close to one that will make the calculations easier.



Fundamentals of Power Systems

PROBLEMS

ANSWER

Select voltage and power base values for each zone.

ASIDE

Zone 1: $S_{B1} = 100 \text{ MVA}$, $V_{B1} = 25 \text{ kV}$

Zone 2: $S_{B2} = 100 \text{ MVA}$, $V_{B2} = 345 \text{ kV}$

Based on these base values, current and impedance base values can also be calculated.

For ZONE 1

$$I_{B1} = \frac{S_{B1}}{\sqrt{3} V_{B1}} = \frac{100 \text{ MVA}}{\sqrt{3} 25 \text{ kV}} = 2309 \text{ A} \qquad Z_{B1} = \frac{V_{B1}^2}{S_{B1}} = \frac{25^2}{100} = 6.25 \Omega$$

For ZONE 2

$$I_{B2} = \frac{S_{B2}}{\sqrt{3} V_{B2}} = \frac{100 \text{ MVA}}{\sqrt{3} 345 \text{ kV}} = 167.3 \text{ A} \qquad Z_{B2} = \frac{V_{B2}^2}{S_{B2}} = \frac{345^2}{100} = 1190 \Omega$$

Fundamentals of Power Systems

PROBLEMS

ANSWER

Converting pu or % values to Ohms

ASIDE

Generator and transformer impedances are given in % or pu. Their base values are calculated on the basis of nominal voltage and apparent power.

$$Z_B = \frac{V_N}{I_N} = \frac{V_N^2}{S_N} \quad \text{where} \quad S_N = I_N V_N$$

It is important to remember that the pu value is calculated by dividing actual value to the base value.

$$Z_{\text{pu}} = \frac{Z_{\text{ACTUAL}}}{Z_B} = Z_{\text{ACTUAL}} \left(\frac{S_N}{V_N^2} \right)$$

This equation can be arranged to obtain the actual value in Ohms from the pu value.

$$Z_{\text{ACTUAL}} = Z_{\text{pu}} Z_B = Z_{\text{pu}} \left(\frac{V_N^2}{S_N} \right)$$

Fundamentals of Power Systems

PROBLEMS

ANSWER

The impedance of the transmission line given in the question can be divided by Z_{B2} and converted to pu value. The impedance of the transmission line can be divided by Z_{B2} and converted to pu value.

$$Z_{pu} = \frac{Z_{ACTUAL}}{Z_B} = \frac{(10 + j45) \Omega}{1190 \Omega}$$

$$Z_{pu} = (0.0084 + j0.0378) \text{ pu} = (0.84 + j3.78) \%$$

Generator and transformer impedances are already given as % or pu. Their base values are the nominal values of the relevant unit. For example, the generator has an impedance of 18% with a base of 50 MVA and 25 kV. These values must be transferred to the new base.

One way to perform this transfer is to first convert the pu values to Ohm values and then divide them by the new base value.

Fundamentals of Power Systems

PROBLEMS

ANSWER

Ohm values of generator and transformer impedances:

$$Z_{G\Omega} = Z_{Gpu} \left(\frac{V_{GN}^2}{S_{GN}} \right) = j0.18 \left(\frac{24^2}{50} \right) = j2.07 \Omega$$

$$Z_{TR\Omega} = Z_{TRpu} \left(\frac{V_{TRN}^2}{S_{TRN}} \right) = j0.12 \left(\frac{25^2}{150} \right) = j0.5 \Omega$$

Now, these Ohm values are converted to pu values using the new bases;

$$Z_{Gpu} = \left(\frac{Z_{G\Omega}}{Z_{B1}} \right) = \frac{j2.07 \Omega}{6.25} = j0.3312 \text{ pu} = j33.12\%$$

$$Z_{TRpu} = \left(\frac{Z_{TR\Omega}}{Z_{B1}} \right) = \frac{j0.5 \Omega}{6.25 \Omega} = j0.08 \text{ pu} = j8\%$$

Fundamentals of Power Systems

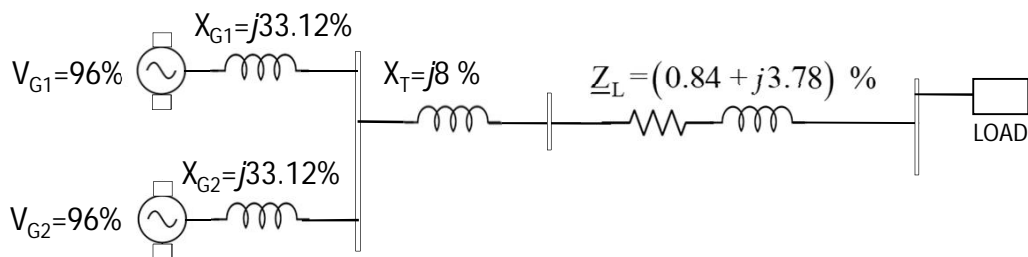
PROBLEMS

ANSWER

Pu value of generator voltage according to new base:

$$V_{G_{pu}} = \left(\frac{V_{GN}}{V_{B1}} \right) = \frac{24}{25} = 0.96 \text{ pu} = 96\%$$

New equivalent impedance circuit with pu and/or % values



Fundamentals of Power Systems

PROBLEMS

QUESTION

A large generator is connected to the grid via a transformer. This type of system is called a unit-linked system. The System data is given as:

Generator:	450 MVA	25 kV	$X_G= 85\%$
Transformer:	500 MVA	25 kV /120 kV	$X_{TR}= 13\%$

Generator and transformer reactances are given in % at their nominal values. These need to be converted to Ohm values.

- Draw a single-line diagram of this system.
- Draw the equivalent circuit of this system by showing the impedances in Ohms.
- Draw the equivalent circuit of this system by showing the impedances with pu values at the base of 500 MVA .
- If a three-phase symmetrical short circuit occurs on the high voltage side of the transformer, what will be the value of the current flowing through the generator windings?

Elektrik Mühendisliđinin Genel Konuları

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Chapter 1 - 49

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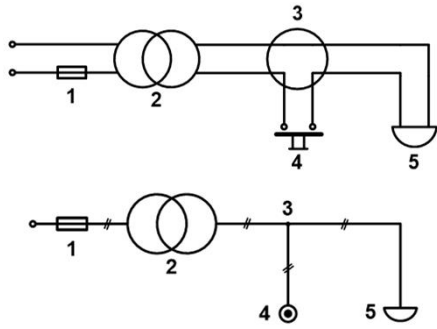
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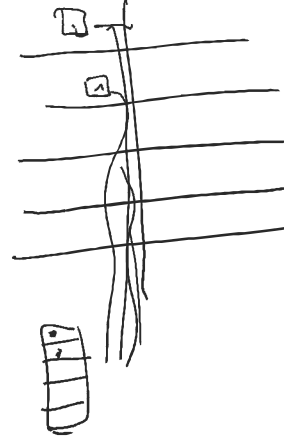
Electric Power Distribution Systems

Chapter 1 - 50

General Topics of Electrical Engineering



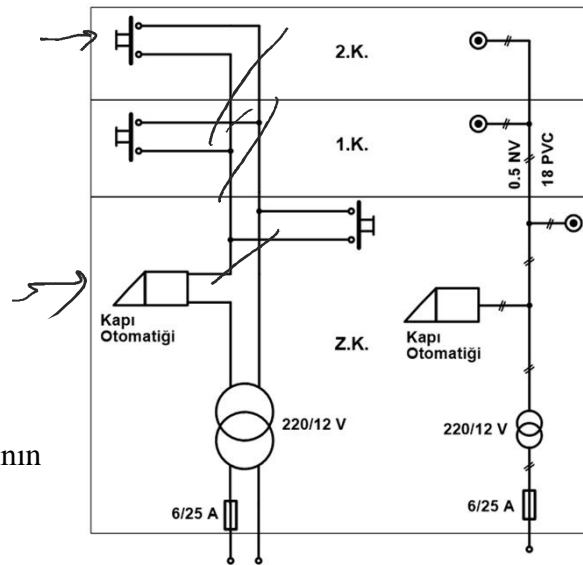
1. Sigorta
2. Zil transformatörü
3. Buat
4. Buton
5. Zil



Şekil. Zil Transformatörü üzerinden beslenen bir zil devresi

İç tesisat yönetmeliğine göre zil devresi, aydınlatma ve priz devresinden ayrı bir sigorta üzerinden beslenmelidir.

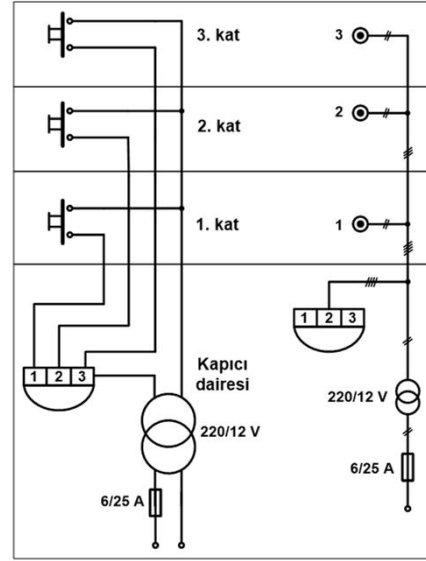
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Şekil. Kapı otomatığı tesisatının açık ve kapalı şeması

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Şekil. Üç katlı bir evde kapıcıyı çağırmak için yapılan numarator tesisatının açık ve kapalı şeması



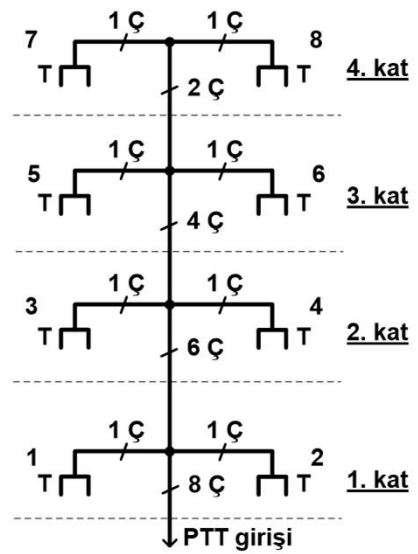
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Chapter 1 - 53

General Topics of Electrical Engineering

Şekil. Dört katlı çift dairesli (8 aboneli) bir binanın telefon tesisatı

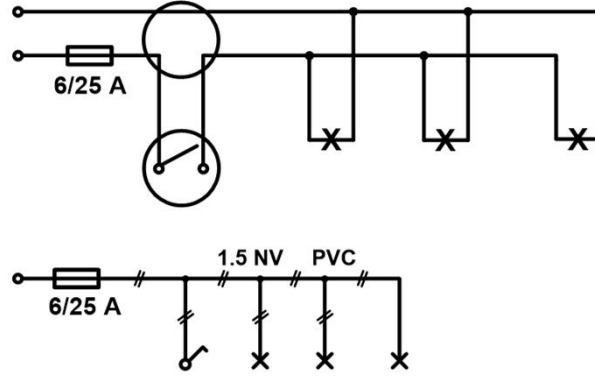


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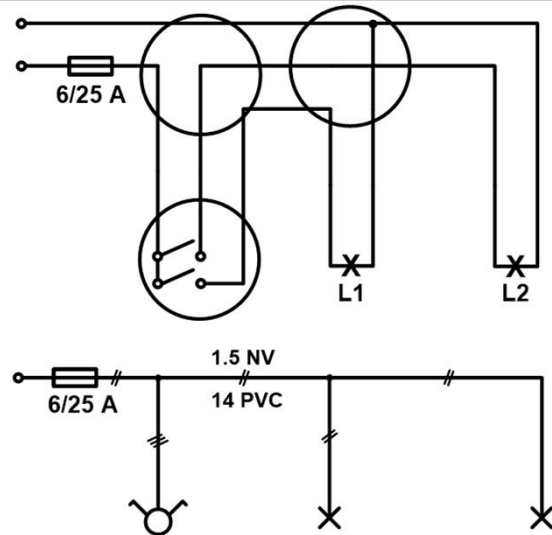
Chapter 1 - 54

General Topics of Electrical Engineering



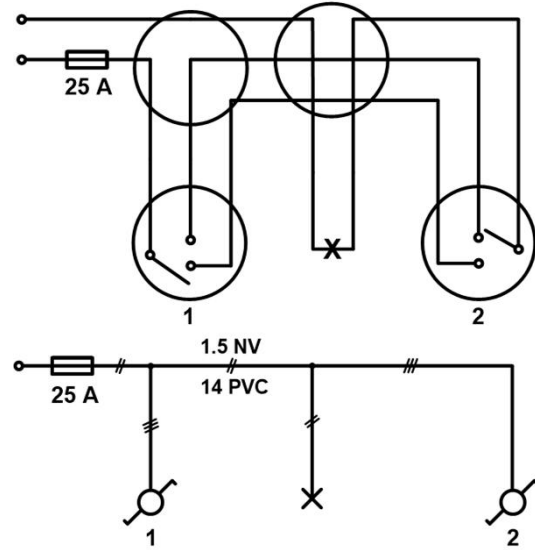
Şekil. Bir lambanın ve 3'lü bir grup lambanın adi anahtarla kumandasının açık ve kapalı şemaları

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Şekil. Komütatör anahtarla yapılan tesisatın açık ve kapalı şeması

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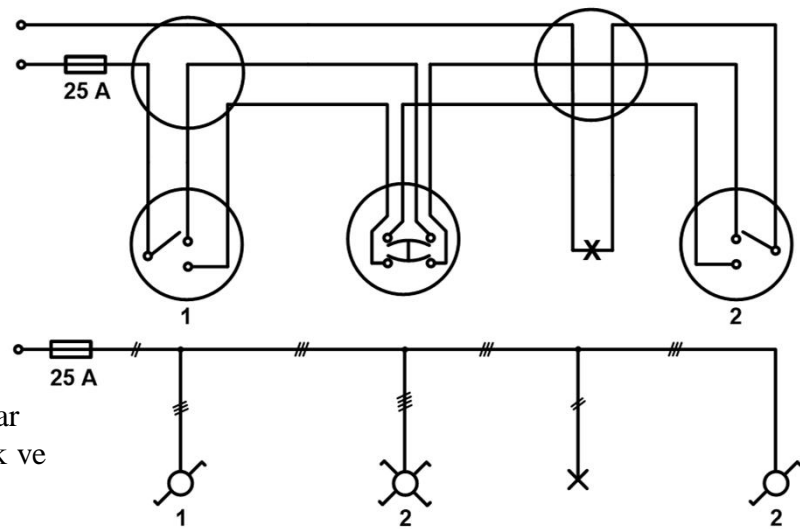
Şekil. Vaviyen anahtar tesisatının açık ve kapalı şeması

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Chapter 1 - 57

General Topics of Electrical Engineering



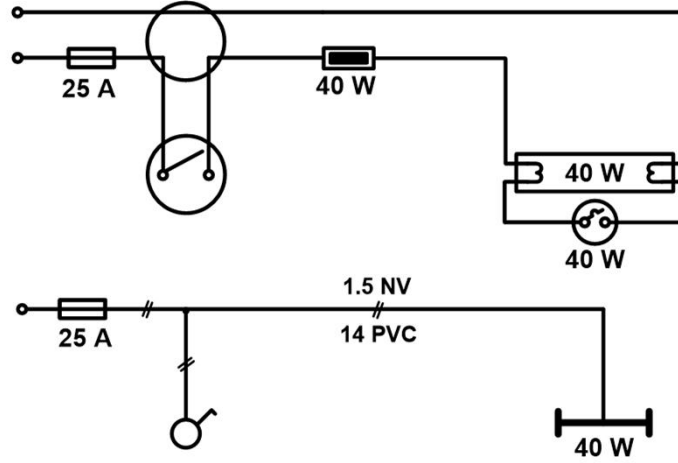
Şekil. Aravaviyen anahtar (Deviyatör) tesisatının açık ve kapalı şeması

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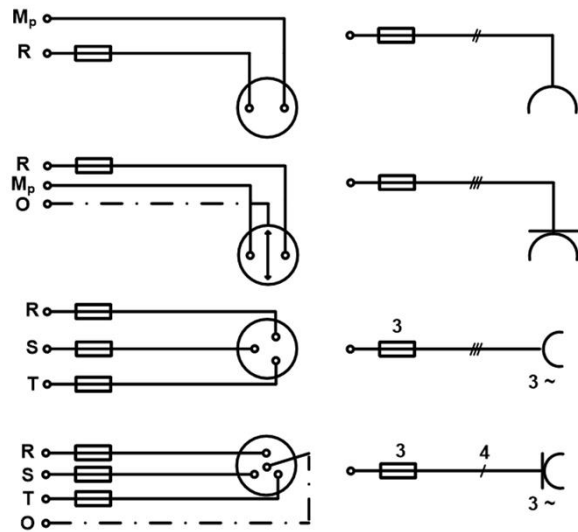
Chapter 1 - 58

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Şekil. Tek flüoresan lampa tesisatı

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Şekil. Bir ve üç fazlı priz devrelerine ait topraksız ve topraklı şemalar

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**End of the Chapter:
Introduction**

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